Ex: Every plant can be peromotived 5 (u,v)= 40+v6 +t for suitable à, b, c for D= R3 Idea: It is just determined y pante (u, v) in 182 vie is, b, i and the equation above Exi compute a parameteration for the parabolaid 2 x2, 232 Alt: There are many ways to parametrice this surface. 5010: 3(xy): (x, y, x2+2y2) p= R2 (010): 5'(10) + (xcos(0), xin(d), (r6s(d)) + 2/sino) - Lreased, romed) - (Itsm2 (0))

D=[0,00) x[0,24] 5013: 5(r,0): (5) reas(d), rsin(d), 222) Ex: Les fit i be a single-variable truston. The surface detrid by moling f a bot the x-axx is parametrical by s (x,0)= Lr, f(x)cos(0), f(x) on(0)) This surface has parametrization 3(x, v) - (x, x 605(0), x 314(0)

11 22/21 Surfaces and Calulus A surface on R3 how the form 5(u,v) = 2xcu, u), y cn,v), 2(u,v) M Some domain DER2 Ex: The tors why major radius 200 and mor radius B (w/ of 1/230)

J 2. ASM 81

is the surface 5(1,1): 1(0+13 car (u) (us (1), (x+13cos (u)) 5m(v))

11/33/31		0
		67
-	I. Targer+ Planes	
	The forger place to surface s'(u, v) at point (a, 6) & 0	
•	the forget place to surface s'(u, v) at point (a, b) & 0 has normal vector li(u, b). Si (a, b) X Sy (a, b)	•
	VB: Su. Law au , and , con also be control and	
ę.	Ex. consider the tons s'(u,v) wil major roder 10 and mor radius 5, what is the target place to s'(u,v) at	
	5" (" 3") what is the target place to 5(u,v) at	
1	St. 5(4.4): 11.	
	501: 5 (U, U): ((10 +5 coscu)) cos(V) (10 +5coscu)) sm(V), 55m(W)	
	5 = 1 - (10 + 5 - 1) 5 = (1) 5	013
volue	5y= L- (10 + 5cos (u)) sin(y), (10+5 cessur) (os(v), 0)	013
	M(u,v): Sulu,v) x5, (u,v) & (no. in principle, we could have	0 3
	i i k (anaed 50 (\$, \$7) x 54 3, 37)	0-7
	Scarlacos v - originamo Suosa	0 1 7
		0 1 2
j j	-10 +casylina) conscardina	0-1-2
		0-1-7
	- Le Cuene	0 1 7
-	= (0-610 4(10+5000) (05 4) 1 - (0-5000 (1) (-(10+5000))	
	+ 1-58 in Luliasy (10 + Scasu) Cosy, Esmash v (10+5 cos w) (smul) K	
	= - 5 cost u) cos (v) [11 + 5 cos (u)];	0.10
-	-5 (05 (n) 5 my (10 + 6 cos (2) / j -5 mu (10 + 5 (05 u) (cos 2 v + m 2 v) K	0 10
		9
-	- (-5(10+5cosul) (cosusos, cosuson, sinu)	9
-	Slavil	9
	Diala.	
		9
		8

「(*14,3 * 14) : (110+5 cos(ま)) cos(ま) (10+5 cos(も)) sm(ま) cos(ま) cos(ま) cos(ま) cos(ま) cos(ま) sm(to sm

15 A = So Isux Sul Great of a parallelogram

Q: where is this coming from?

A: Premise approximation of surfaces via possible ograms limiting these approximations yields that he mula

The surface are of a surface of (u,v) parametrized in domain D

Ab forthis to north, we assume that I (u, i) transver the antace once on p. (v. milar to relength rocks cover to be stravered once)

Exi compute the serface over of the true of major radius to and minor rodus 5

Soli or already compated n (u,v) = 30 (1,v)

Now at the point;

I surface area

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22/11 ((u,v) x 5, (u, x) = 1-5(1015con) [cos2cor2 +cos2cor2 + cos2cor2 + cos2cor2 25/2+cosu / Jeas 26/1/2003 (4)+ cor 26/1/ + sin 26/1) 52 (5 + CO22M) Area(s): (Tocs) 15, 45, 1 dA = 127 128 a 6(a trosa) dudu 25 1 (2+con) [v] 2 du - 50 H (du + SM (u)) | 277 - 56 H (2(2H-0) + (0-01) U-6 -200 H2 Exercise comple the surface area of a general tons of major radus dars monor radus & (shall be 40 BT2) NB: If f(x,y) is a function the graph is a number of (x,y) = exity, f(x,y). The round recor to that surface is ricking). Six Sy = det | 1 | Fx | - (-Fx, -Fy 1) · Areal groph (4)): No Stx + 5° +1 det Idea dutace one is an area. So we shall by analogy to previous you) be able to unte Area (S): SIS 1 ds

resembly former A(R): SIS 1 dA,

to make analogy warn, ds = 1 du x syldet NB: Is x si lis a Jacobian.

by stars on doman D is

Sof de = Sof (s(u, v)) | six xsilds

Do Sof dr = f (r (+)) | r'(+) | d+ w/ne negron

Each piece is replaced by a 2-diversaral conserport.